



Magruder Statistics:

Homogeneity Screening

Heterogeneity among the sample units ($\sigma^2_{\text{Samples}}$) can inflate the spread in sample results. This can mask the true Lab Bias and interferes with Z scores.

Sources of Variance for Check Sample Results can be expressed as follows:

$$\sigma^2_{\text{Sample Results}} = \sigma^2_{\text{Analytical}} + \sigma^2_{\text{Labs}} + \sigma^2_{\text{Samples}}$$

Ideally, to test for sample homogeneity we need to minimize the analytical variance ($\sigma^2_{\text{Analytical}}$) and the Lab Bias (σ^2_{Labs}) and isolate the variance due to the sample units ($\sigma^2_{\text{Samples}}$).

Reduced Lab Bias is achieved using a single Lab!

Can We Estimate Homogeneity From the CSP Data?

- In N₂ by Combustion we have a very precise method with over 50 Analysts consistently reporting **Reproducibility < 2 %RSD** and **Repeatability < 1 %rsd** for each sample.
- This is an extremely narrow dispersion (Bias) for so many Labs.
- So looking at our sources of variance again:
 - Reproducibility is heavily reflected in σ_{Labs} **and is low!**
 - Repeatability is essentially the $\sigma_{\text{Analytical}}$ **and is low!**

$$\sigma_{\text{Sample Results}}^2 = \sigma_{\text{Analytical}}^2 + \sigma_{\text{Labs}}^2 + \sigma_{\text{Samples}}^2$$

**No other Analyte
Methods have a
consistently low
bias as with
 N_2 by Combustion!**

**If this gets out-of-line, we have
reason to question the Homogeneity.**



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Questions?